

# Beta-blockers - Discrete Mixture Models

February 8, 2012

The data set "betablockers" is loaded from the package "flexmix".

```
> library(flexmix)
> data(betablocker)
> betablocker$Treatment <- as.factor(betablocker$Treatment)
```

First a simple logit model is fitted with the only covariate "Treatment".

```
> GlmT <- glm(cbind(Deaths, Total - Deaths) ~ Treatment, family = "binomial",
+ data = betablocker)
> summary(GlmT)
```

Call:

```
glm(formula = cbind(Deaths, Total - Deaths) ~ Treatment, family = "binomial",
     data = betablocker)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-5.316	-1.492	-0.134	1.707	5.856

Coefficients:

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-2.1971	0.0336	-65.42	< 2e-16 ***
TreatmentTreated	-0.2574	0.0494	-5.21	1.9e-07 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 332.99 on 43 degrees of freedom  
Residual deviance: 305.76 on 42 degrees of freedom  
AIC: 527.2

Number of Fisher Scoring iterations: 4

Now the logit model is extended by the factor "Center" which has 22 different values. The deviance reduces from 305.76 with 42 degrees of freedom to 23.62 with 21 degrees of freedom.

```
> GlmTC <- glm(cbind(Deaths, Total - Deaths) ~ Treatment + as.factor(Center),
+             family = "binomial", data = betablocker)
> summary(GlmTC)
```

Call:

```
glm(formula = cbind(Deaths, Total - Deaths) ~ Treatment + as.factor(Center),
     family = "binomial", data = betablocker)
```

Deviance Residuals:

```
      Min       1Q   Median       3Q      Max
-1.828  -0.618   0.004   0.535   1.921
```

Coefficients:

	Estimate	Std. Error	z value	Pr(> z )	
(Intercept)	-2.3493	0.4260	-5.52	3.5e-08	***
TreatmentTreated	-0.2610	0.0499	-5.23	1.7e-07	***
as.factor(Center)2	0.1739	0.4832	0.36	0.719	
as.factor(Center)3	0.2428	0.5004	0.49	0.628	
as.factor(Center)4	-0.0391	0.4309	-0.09	0.928	
as.factor(Center)5	-0.0217	0.4480	-0.05	0.961	
as.factor(Center)6	0.1685	0.5395	0.31	0.755	
as.factor(Center)7	0.5966	0.4308	1.38	0.166	
as.factor(Center)8	0.2715	0.4373	0.62	0.535	
as.factor(Center)9	0.3888	0.4462	0.87	0.384	
as.factor(Center)10	0.0958	0.4293	0.22	0.823	
as.factor(Center)11	0.0520	0.4363	0.12	0.905	
as.factor(Center)12	0.9153	0.4406	2.08	0.038	*
as.factor(Center)13	-0.6357	0.4720	-1.35	0.178	
as.factor(Center)14	-0.3065	0.4375	-0.70	0.484	
as.factor(Center)15	1.0016	0.4505	2.22	0.026	*
as.factor(Center)16	0.8799	0.4449	1.98	0.048	*
as.factor(Center)17	0.3997	0.4573	0.87	0.382	
as.factor(Center)18	-0.5635	0.5059	-1.11	0.265	
as.factor(Center)19	-1.0144	0.5436	-1.87	0.062	.
as.factor(Center)20	0.8759	0.4447	1.97	0.049	*
as.factor(Center)21	0.1966	0.4436	0.44	0.658	
as.factor(Center)22	-0.5812	0.4451	-1.31	0.192	

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

```
Null deviance: 332.993 on 43 degrees of freedom
Residual deviance: 23.621 on 21 degrees of freedom
AIC: 287.1
```

Number of Fisher Scoring iterations: 4

In the following two mixed models are fitted with Gauss-Hermite-Quadrature, so "glmmML" is needed.

```
> library(glmML)
```

First the random intercept model with 4 quadrature points is fitted.

```
> MixedGH4 <- glmML(cbind(Deaths, Total - Deaths) ~ Treatment, cluster=Center,
+                   method = c("ghq"), n.points = 4, boot = 0, data=betablocker)
> summary(MixedGH4)
```

```
Call: glmML(formula = cbind(Deaths, Total - Deaths) ~ Treatment, data = betablocker,
```

	coef	se(coef)	z	Pr(> z )
(Intercept)	-2.196	0.1131	-19.42	0.0e+00
TreatmentTreated	-0.261	0.0499	-5.23	1.7e-07

```
Scale parameter in mixing distribution: 0.487 gaussian
Std. Error: 0.084
```

```
LR p-value for H_0: sigma = 0: 9.28e-47
```

```
Residual deviance: 101 on 41 degrees of freedom AIC: 107
```

Now we use 20 quadrature points but there is no big difference in coefficients.

```
> MixedGH20 <- glmML(cbind(Deaths, Total - Deaths) ~ Treatment, cluster=Center,
+                   method = c("ghq"), n.points = 20, boot = 0, data=betablocker)
> summary(MixedGH20)
```

```
Call: glmML(formula = cbind(Deaths, Total - Deaths) ~ Treatment, data = betablocker,
```

	coef	se(coef)	z	Pr(> z )
(Intercept)	-2.196	0.1131	-19.42	0.0e+00
TreatmentTreated	-0.261	0.0499	-5.23	1.7e-07

```
Scale parameter in mixing distribution: 0.487 gaussian
Std. Error: 0.0841
```

```
LR p-value for H_0: sigma = 0: 9.28e-47
```

```
Residual deviance: 101 on 41 degrees of freedom AIC: 107
```

```
> set.seed(5)
```

Finally we fit the discrete mixture models for which the function "stepFlexmix" is used. Here we use three components defined by option "k=3".

```
> detach(package:glmML)
```

```
> MixFix3 <- stepFlexmix(cbind(Deaths, Total - Deaths) ~ 1 | Center, model =
+ FLXMRglmfix(family = "binomial", fixed = ~ Treatment), k = 3, nrep = 5,
+ data = betablocker)
```

```
3 : * * * * *
```

Typing the name of the fitted model yields the sizes of the three clusters.

```
> MixFix3
```

Call:

```
stepFlexmix(cbind(Deaths, Total - Deaths) ~ 1 | Center, model = FLXMRglmfix(family = "binomial",  
  fixed = ~Treatment), data = betablocker, k = 3, nrep = 5)
```

Cluster sizes:

```
 1  2  3  
24 10 10
```

convergence after 12 iterations

The coefficients are printed by the command "parameters()".

```
> parameters(MixFix3)
```

```
                Comp.1 Comp.2 Comp.3  
coef.TreatmentTreated -0.258 -0.258 -0.258  
coef.(Intercept)      -2.250 -2.834 -1.610
```

The command "summary()" returns for example the estimated component weights and the BIC. The coefficients with standard errors and p-values can be found by "summary(refit())".

```
> library(flexmix)
```

```
> summary(MixFix3)
```

Call:

```
stepFlexmix(cbind(Deaths, Total - Deaths) ~ 1 | Center, model = FLXMRglmfix(family = "binomial",  
  fixed = ~Treatment), data = betablocker, k = 3, nrep = 5)
```

```
      prior size post>0 ratio  
Comp.1 0.512   24     32 0.750  
Comp.2 0.239   10     20 0.500  
Comp.3 0.249   10     22 0.455
```

```
'log Lik.' -159 (df=6)
```

```
AIC: 331   BIC: 341
```

```
> summary(refit(MixFix3))
```

```
$Comp.1
```

```
      Estimate Std. Error z value Pr(>|z|)  
TreatmentTreated -0.2582    0.0499  -5.17 2.3e-07 ***  
(Intercept)      -2.2502    0.0405 -55.52 < 2e-16 ***  
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```

$Comp.2
              Estimate Std. Error z value Pr(>|z|)
TreatmentTreated -0.2582    0.0499  -5.17  2.3e-07 ***
(Intercept)      -2.8337    0.0751 -37.74 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

$Comp.3
              Estimate Std. Error z value Pr(>|z|)
TreatmentTreated -0.2582    0.0499  -5.17  2.3e-07 ***
(Intercept)      -1.6097    0.0557 -28.88 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```
> set.seed(5)
```

Finally the discrete mixture model with 4 components is fitted.

```

> MixFix4 <- stepFlexmix(cbind(Deaths, Total - Deaths) ~ 1 | Center, model =
+   FLXMRglmfix(family = "binomial", fixed = ~Treatment), k = 4, nrep = 5,
+   data = betablocker)

```

```
4 : * * * * *
```

```
> MixFix4
```

Call:

```
stepFlexmix(cbind(Deaths, Total - Deaths) ~ 1 | Center, model = FLXMRglmfix(family = "binomial",
fixed = ~Treatment), data = betablocker, k = 4, nrep = 5)
```

Cluster sizes:

```

 1  2  3  4
24  2  8 10

```

convergence after 13 iterations

```
> parameters(MixFix4)
```

```

              Comp.1 Comp.2 Comp.3 Comp.4
coef.TreatmentTreated -0.258 -0.258 -0.258 -0.258
coef.(Intercept)      -2.258 -1.786 -1.440 -2.833

```

```
> summary(MixFix4)
```

Call:

```
stepFlexmix(cbind(Deaths, Total - Deaths) ~ 1 | Center, model = FLXMRglmfix(family = "binomial",
fixed = ~Treatment), data = betablocker, k = 4, nrep = 5)
```

```

              prior size post>0 ratio
Comp.1 0.4820   24      32 0.7500
Comp.2 0.0988    2      26 0.0769

```

```
Comp.3 0.1796 8 20 0.4000
Comp.4 0.2396 10 20 0.5000
```

```
'log Lik.' -156 (df=8)
AIC: 328 BIC: 342
```

```
> summary(refit(MixFix4))
```

```
$Comp.1
```

	Estimate	Std. Error	z value	Pr(> z )
TreatmentTreated	-0.2584	0.0499	-5.18	2.2e-07 ***
(Intercept)	-2.2578	0.0430	-52.50	< 2e-16 ***

```
---
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$Comp.2
```

	Estimate	Std. Error	z value	Pr(> z )
TreatmentTreated	-0.2584	0.0499	-5.18	2.2e-07 ***
(Intercept)	-1.7872	0.0834	-21.42	< 2e-16 ***

```
---
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$Comp.3
```

	Estimate	Std. Error	z value	Pr(> z )
TreatmentTreated	-0.2584	0.0499	-5.18	2.2e-07 ***
(Intercept)	-1.4395	0.0700	-20.57	< 2e-16 ***

```
---
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$Comp.4
```

	Estimate	Std. Error	z value	Pr(> z )
TreatmentTreated	-0.2584	0.0499	-5.18	2.2e-07 ***
(Intercept)	-2.8333	0.0751	-37.71	< 2e-16 ***

```
---
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```